



University of Kelaniya – Sri Lanka

External Examinations Branch

Bachelor of Commerce (Special) Degree Second Examination (External)- 2010 December 2011/ January 2012

Faculty of Commerce and Management

BCOME 2035 – Business Statistics

No. of questions: Seven (07)

Time: 03 hours

Answer any five (05) questions.

Graph papers and statistical tables are provided. Use of calculators will be allowed.

(01) a) How do you define the word statistics?

(02 marks)

b) What is meant by statistical investigation? What are the main steps in statistical investigation.

(03 marks)

c) Explain the difference between descriptive statistics and inferential statistics.

(03 marks)

d) Explain the following terms using suitable examples.

(i). Population

(ii). Sample

(iii). Sample statistics

(iv). Parameter

(v). Qualitative variable

(vi). Quantitative variable

(12 marks)

(Total 20 marks)

(02) a) (i) Distinguish between measures of central tendency and measures of dispersion.

(05 marks)

(ii) "When describing the measures of variability, the mean deviation is calculated by using absolute values of the deviations". Do you agree with this statement. Explain the reasons for your answer.

(05 marks)

b) You are given the following computer solution in relation to some sample data.

| <u>N</u> | <u>MEAN</u> | <u>MEDIAN</u> | <u>SITDEU</u> | <u>SEMEAN</u> | <u>MIN</u> | <u>MAX</u> | <u>Q1</u> | <u>Q3</u> |
|----------|-------------|---------------|---------------|---------------|------------|------------|-----------|-----------|
| 12 | 24 | 26 | 15.61 | 4.94 | 4.00 | 48.00 | 7.75 | 37.75 |

(i) How many numbers of observations are there in the sample.

(02 marks)

(ii) State the range and semi-inter quartile range of the sample.

(04 marks)

(iii) Find the variance and coefficient of variation for the above data.

(04 marks)

(Total 20 marks)

(03) a) (i) What is the importance of constructing models for time series data.

(04 marks)

(ii) Describe any two models which are having for time series data.

(04 marks)

b) How do irregular variations of time series differ from cyclical movements?

(04 marks)

c) Following are given income of sales of a certain firm according to the consecutive years.

| Year | Income of sales (in 000' Rs.) |
|------|----------------------------------|
| 1996 | 2.6 |
| 1997 | 2.5 |
| 1998 | 2.3 |
| 1999 | 3.2 |
| 2000 | 2.9 |
| 2001 | 3.2 |
| 2002 | 3.3 |
| 2003 | 3.6 |
| 2004 | 3.8 |
| 2005 | 3.7 |
| 2006 | 3.4 |
| 2007 | 3.6 |
| 2008 | 4.0 |
| 2009 | 4.2 |
| 2010 | 4.5 |

(i) Construct a scatter plot using above data.

(02 marks)

(ii) Derive trend line using least square estimation method.

(04 marks)

(iii) Forecast the sales for the year 2011.

(02 marks)

(Total 20 marks)

(04) a) What is the difference between “probability” and “probability distribution”. (04 marks)

b) Verify that the following distribution can be considered as a probability distribution.
Give reasons for your answer.

| | | | | | | |
|-------|-----|-----|-----|------|-----|------|
| X | 0 | 1 | 2 | 3 | 4 | 5 |
| P (X) | 0.1 | 0.5 | 0.2 | 0.15 | 0.1 | 0.05 |

(03 marks)

c) Following probability distribution shows the weekly demand for tea.

| | | | |
|------------------|-----|-----|-----|
| Demand (X) | 0 | 1 | 2 |
| Probability P(X) | 0.3 | 0.5 | 0.2 |

(i) Determine the expected demand for tea.

(ii) Find the variance and standard deviation of weekly demand for tea.

(04 marks)

d) Explain the main characteristics of the following probability distributions.

Binomial distribution
Poisson distribution
Normal distribution

(09 marks)

(Total 20 marks)

(05) Daily expenditure on food and housing of 10 house hold groups in a particular year are as follows.

| Expenses for food (‘000 Rs) | Expenses for housing (‘000 Rs) |
|--------------------------------|-----------------------------------|
| 9.2 | 4.3 |
| 9.3 | 3.9 |
| 9.5 | 5.2 |
| 8.9 | 5.1 |
| 9.7 | 5.4 |
| 8.7 | 4.7 |
| 10.1 | 6.9 |
| 9.4 | 5.5 |
| 9.8 | 3.6 |
| 9.7 | 4.2 |

a) Can it be seen positive relationship between food & housing expenditures.

(03 marks)

b) Construct regression equation between food expenses and housing expenditures, using least square estimation method.

(08 marks)

- c) What is coefficient of determination?
(02 marks)
- d) Compute coefficient of determination for the above data.
(04 marks)
- e) What is the importance of testing the statistical significance for the above data.
(03 marks)
(Total 20 marks)

(06) a) What are the main areas of statistical inference.
(02 marks)

b) Explain why statistical inference is important in Business Statistics?
(04 marks)

c) Briefly explain “interval estimation”. What are the two main components on interval estimation.
(04 marks)

d) Explain any two of the followings;
(i) Consistency
(ii) Efficiency
(iii) Unbiasedness
(04 marks)

e) Forty children participated to an eye clinic. A random sample of 10 children were selected and measured their weights. Below are given the results (weight in kilograms)
98, 65, 90, 112, 70 60, 50, 49, 35, 89

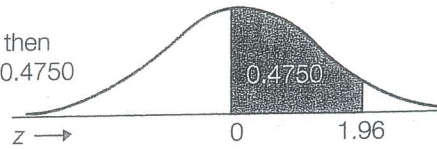
Construct a 95% confidence interval for the population mean weight.
(06 marks)
(Total 20 marks)

(07) Explain the followings using practical examples.
(i) Sampling methods
(ii) Statistical quality control
(iii) Price indexes
(iv) Quantity indexes
(05 x 04 = 20 marks)

APPENDIX D

Areas under the Normal Curve

Example:
If $z = 1.96$, then
 $P(0 \text{ to } z) = 0.4750$



| z | 0.00 | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |
|-----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 0.0 | 0.0000 | 0.0040 | 0.0080 | 0.0120 | 0.0160 | 0.0199 | 0.0239 | 0.0279 | 0.0319 | 0.0359 |
| 0.1 | 0.0398 | 0.0438 | 0.0478 | 0.0517 | 0.0557 | 0.0596 | 0.0636 | 0.0675 | 0.0714 | 0.0753 |
| 0.2 | 0.0793 | 0.0832 | 0.0871 | 0.0910 | 0.0948 | 0.0987 | 0.1026 | 0.1064 | 0.1103 | 0.1141 |
| 0.3 | 0.1179 | 0.1217 | 0.1255 | 0.1293 | 0.1331 | 0.1368 | 0.1406 | 0.1443 | 0.1480 | 0.1517 |
| 0.4 | 0.1554 | 0.1591 | 0.1628 | 0.1664 | 0.1700 | 0.1736 | 0.1772 | 0.1808 | 0.1844 | 0.1879 |
| 0.5 | 0.1915 | 0.1950 | 0.1985 | 0.2019 | 0.2054 | 0.2088 | 0.2123 | 0.2157 | 0.2190 | 0.2224 |
| 0.6 | 0.2257 | 0.2291 | 0.2324 | 0.2357 | 0.2389 | 0.2422 | 0.2454 | 0.2486 | 0.2517 | 0.2549 |
| 0.7 | 0.2580 | 0.2611 | 0.2642 | 0.2673 | 0.2704 | 0.2734 | 0.2764 | 0.2794 | 0.2823 | 0.2852 |
| 0.8 | 0.2881 | 0.2910 | 0.2939 | 0.2967 | 0.2995 | 0.3023 | 0.3051 | 0.3078 | 0.3106 | 0.3133 |
| 0.9 | 0.3159 | 0.3186 | 0.3212 | 0.3238 | 0.3264 | 0.3289 | 0.3315 | 0.3340 | 0.3365 | 0.3389 |
| 1.0 | 0.3413 | 0.3438 | 0.3461 | 0.3485 | 0.3508 | 0.3531 | 0.3554 | 0.3577 | 0.3599 | 0.3621 |
| 1.1 | 0.3643 | 0.3665 | 0.3686 | 0.3708 | 0.3729 | 0.3749 | 0.3770 | 0.3790 | 0.3810 | 0.3830 |
| 1.2 | 0.3849 | 0.3869 | 0.3888 | 0.3907 | 0.3925 | 0.3944 | 0.3962 | 0.3980 | 0.3997 | 0.4015 |
| 1.3 | 0.4032 | 0.4049 | 0.4066 | 0.4082 | 0.4099 | 0.4115 | 0.4131 | 0.4147 | 0.4162 | 0.4177 |
| 1.4 | 0.4192 | 0.4207 | 0.4222 | 0.4236 | 0.4251 | 0.4265 | 0.4279 | 0.4292 | 0.4306 | 0.4319 |
| 1.5 | 0.4332 | 0.4345 | 0.4357 | 0.4370 | 0.4382 | 0.4394 | 0.4406 | 0.4418 | 0.4429 | 0.4441 |
| 1.6 | 0.4452 | 0.4463 | 0.4474 | 0.4484 | 0.4495 | 0.4505 | 0.4515 | 0.4525 | 0.4535 | 0.4545 |
| 1.7 | 0.4554 | 0.4564 | 0.4573 | 0.4582 | 0.4591 | 0.4599 | 0.4608 | 0.4616 | 0.4625 | 0.4633 |
| 1.8 | 0.4641 | 0.4649 | 0.4656 | 0.4664 | 0.4671 | 0.4678 | 0.4686 | 0.4693 | 0.4699 | 0.4706 |
| 1.9 | 0.4713 | 0.4719 | 0.4726 | 0.4732 | 0.4738 | 0.4744 | 0.4750 | 0.4756 | 0.4761 | 0.4767 |
| 2.0 | 0.4772 | 0.4778 | 0.4783 | 0.4788 | 0.4793 | 0.4798 | 0.4803 | 0.4808 | 0.4812 | 0.4817 |
| 2.1 | 0.4821 | 0.4826 | 0.4830 | 0.4834 | 0.4838 | 0.4842 | 0.4846 | 0.4850 | 0.4854 | 0.4857 |
| 2.2 | 0.4861 | 0.4864 | 0.4868 | 0.4871 | 0.4875 | 0.4878 | 0.4881 | 0.4884 | 0.4887 | 0.4890 |
| 2.3 | 0.4893 | 0.4896 | 0.4898 | 0.4901 | 0.4904 | 0.4906 | 0.4909 | 0.4911 | 0.4913 | 0.4916 |
| 2.4 | 0.4918 | 0.4920 | 0.4922 | 0.4925 | 0.4927 | 0.4929 | 0.4931 | 0.4932 | 0.4934 | 0.4936 |
| 2.5 | 0.4938 | 0.4940 | 0.4941 | 0.4943 | 0.4945 | 0.4946 | 0.4948 | 0.4949 | 0.4951 | 0.4952 |
| 2.6 | 0.4953 | 0.4955 | 0.4956 | 0.4957 | 0.4959 | 0.4960 | 0.4961 | 0.4962 | 0.4963 | 0.4964 |
| 2.7 | 0.4965 | 0.4966 | 0.4967 | 0.4968 | 0.4969 | 0.4970 | 0.4971 | 0.4972 | 0.4973 | 0.4974 |
| 2.8 | 0.4974 | 0.4975 | 0.4976 | 0.4977 | 0.4977 | 0.4978 | 0.4979 | 0.4979 | 0.4980 | 0.4981 |
| 2.9 | 0.4981 | 0.4982 | 0.4982 | 0.4983 | 0.4984 | 0.4984 | 0.4985 | 0.4985 | 0.4986 | 0.4986 |
| 3.0 | 0.4987 | 0.4987 | 0.4987 | 0.4988 | 0.4988 | 0.4989 | 0.4989 | 0.4989 | 0.4990 | 0.4990 |

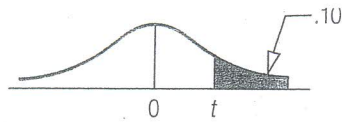
APPENDIX E

Table of Random Numbers

| | | | | | | | | | |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 02711 | 08182 | 75997 | 79866 | 58095 | 83319 | 80295 | 79741 | 74599 | 84379 |
| 94873 | 90935 | 31684 | 63952 | 09865 | 14491 | 99518 | 93394 | 34691 | 14985 |
| 54921 | 78680 | 06635 | 98689 | 17306 | 25170 | 65928 | 87709 | 30533 | 89736 |
| 77640 | 97636 | 37397 | 93379 | 56454 | 59818 | 45827 | 74164 | 71666 | 46977 |
| 61545 | 00835 | 93251 | 87203 | 36759 | 49197 | 85967 | 01704 | 19634 | 21898 |
| 17147 | 19519 | 22497 | 16857 | 42426 | 84822 | 92598 | 49186 | 88247 | 39967 |
| 13748 | 04742 | 92460 | 85801 | 53444 | 65626 | 58710 | 55406 | 17173 | 69776 |
| 87455 | 14813 | 50373 | 28037 | 91182 | 32786 | 65261 | 11173 | 34376 | 36408 |
| 08999 | 57409 | 91185 | 10200 | 61411 | 23392 | 47797 | 56377 | 71635 | 08601 |
| 78804 | 81333 | 53809 | 32471 | 46034 | 36306 | 22498 | 19239 | 85428 | 55721 |
| 82173 | 26921 | 28472 | 98958 | 07960 | 66124 | 89731 | 95069 | 18625 | 92405 |
| 97594 | 25168 | 89178 | 68190 | 05043 | 17407 | 48201 | 83917 | 11413 | 72920 |
| 73881 | 67176 | 93504 | 42636 | 38233 | 16154 | 96451 | 57925 | 29667 | 30859 |
| 46071 | 22912 | 90326 | 42453 | 88108 | 72064 | 58601 | 32357 | 90610 | 32921 |
| 44492 | 19686 | 12495 | 93135 | 95185 | 77799 | 52441 | 88272 | 22024 | 80631 |
| 31864 | 72170 | 37722 | 55794 | 14636 | 05148 | 54505 | 50113 | 21119 | 25228 |
| 51574 | 90692 | 43339 | 65689 | 76539 | 27909 | 05467 | 21727 | 51141 | 72949 |
| 35350 | 76132 | 92925 | 92124 | 92634 | 35681 | 43690 | 89136 | 35599 | 84138 |
| 46943 | 36502 | 01172 | 46045 | 46991 | 33804 | 80006 | 35542 | 61056 | 75666 |
| 22665 | 87226 | 33304 | 57975 | 03985 | 21566 | 65796 | 72915 | 81466 | 89205 |
| 39437 | 97957 | 11838 | 10433 | 21564 | 51570 | 73558 | 27495 | 34533 | 57808 |
| 77082 | 47784 | 40098 | 97962 | 89845 | 28392 | 78187 | 06112 | 08169 | 11261 |
| 24544 | 25649 | 43370 | 28007 | 06779 | 72402 | 62632 | 53956 | 24709 | 06978 |
| 27503 | 15558 | 37738 | 24849 | 70722 | 71859 | 83736 | 06016 | 94397 | 12529 |
| 24590 | 24545 | 06435 | 52758 | 45685 | 90151 | 46516 | 49644 | 92686 | 84870 |
| 48155 | 86226 | 40359 | 28723 | 15364 | 69125 | 12609 | 57171 | 86857 | 31702 |
| 20226 | 53752 | 90648 | 24362 | 83314 | 00014 | 19207 | 69413 | 97016 | 86290 |
| 70178 | 73444 | 38790 | 53626 | 93780 | 18629 | 68766 | 24371 | 74639 | 30782 |
| 10169 | 41465 | 51935 | 05711 | 09799 | 79077 | 88159 | 33437 | 68519 | 03040 |
| 81084 | 03701 | 28598 | 70013 | 63794 | 53169 | 97054 | 60303 | 23259 | 96196 |
| 69202 | 20777 | 21727 | 81511 | 51887 | 16175 | 53746 | 46516 | 70339 | 62727 |
| 80561 | 95787 | 89426 | 93325 | 86412 | 57479 | 54194 | 52153 | 19197 | 81877 |
| 08199 | 26703 | 95128 | 48599 | 09333 | 12584 | 24374 | 31232 | 61782 | 44032 |
| 98883 | 28220 | 39358 | 53720 | 80161 | 83371 | 15181 | 11131 | 12219 | 55920 |
| 84568 | 69286 | 76054 | 21615 | 80883 | 36797 | 82845 | 39139 | 90900 | 18172 |
| 04269 | 35173 | 95745 | 53893 | 86022 | 77722 | 52498 | 84193 | 22448 | 22571 |
| 10538 | 13124 | 36099 | 13140 | 37706 | 44562 | 57179 | 44693 | 67877 | 01549 |
| 77843 | 24955 | 25900 | 63843 | 95029 | 93859 | 93634 | 20205 | 66294 | 41218 |
| 12034 | 94636 | 49455 | 76362 | 83532 | 31062 | 69903 | 91186 | 65768 | 55949 |
| 10524 | 72829 | 47641 | 93315 | 80875 | 28090 | 97728 | 52560 | 34937 | 79548 |
| 68935 | 76632 | 46984 | 61772 | 92786 | 22651 | 07086 | 89754 | 44143 | 97687 |
| 89450 | 65665 | 29190 | 43709 | 11172 | 34481 | 95977 | 47535 | 25658 | 73898 |
| 90696 | 20451 | 24211 | 97310 | 60446 | 73530 | 62865 | 96574 | 13829 | 72226 |
| 49006 | 32047 | 93086 | 00112 | 20470 | 17136 | 28255 | 86328 | 07293 | 38809 |
| 74591 | 87025 | 52368 | 59416 | 34417 | 70557 | 86746 | 55809 | 53628 | 12000 |
| 06315 | 17012 | 77103 | 00968 | 07235 | 10728 | 42189 | 33292 | 51487 | 64443 |
| 62386 | 09184 | 62092 | 46617 | 99419 | 64230 | 95034 | 85481 | 07857 | 42510 |
| 86848 | 82122 | 04028 | 36959 | 87827 | 12813 | 08627 | 80699 | 13345 | 51695 |
| 65643 | 69480 | 46598 | 04501 | 40403 | 91408 | 32343 | 48130 | 49303 | 90689 |
| 11084 | 46534 | 78957 | 77353 | 39578 | 77868 | 22970 | 84349 | 09184 | 70603 |

APPENDIX F

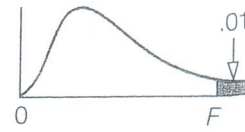
Student's t Distribution



| df | Level of Significance for One-Tailed Test | | | | | |
|-----|---|-------|--------|--------|--------|---------|
| | 0.100 | 0.050 | 0.025 | 0.010 | 0.005 | 0.0005 |
| | Level of Significance for Two-Tailed Test | | | | | |
| | 0.20 | 0.10 | 0.05 | 0.02 | 0.01 | 0.001 |
| 1 | 3.078 | 6.314 | 12.706 | 31.821 | 63.657 | 636.619 |
| 2 | 1.886 | 2.920 | 4.303 | 6.965 | 9.925 | 31.599 |
| 3 | 1.638 | 2.353 | 3.182 | 4.541 | 5.841 | 12.924 |
| 4 | 1.533 | 2.132 | 2.776 | 3.747 | 4.604 | 8.610 |
| 5 | 1.476 | 2.015 | 2.571 | 3.365 | 4.032 | 6.869 |
| 6 | 1.440 | 1.943 | 2.447 | 3.143 | 3.707 | 5.959 |
| 7 | 1.415 | 1.895 | 2.365 | 2.998 | 3.499 | 5.408 |
| 8 | 1.397 | 1.860 | 2.306 | 2.896 | 3.355 | 5.041 |
| 9 | 1.383 | 1.833 | 2.262 | 2.821 | 3.250 | 4.781 |
| 10 | 1.372 | 1.812 | 2.228 | 2.764 | 3.169 | 4.587 |
| 11 | 1.363 | 1.796 | 2.201 | 2.718 | 3.106 | 4.437 |
| 12 | 1.356 | 1.782 | 2.179 | 2.681 | 3.055 | 4.318 |
| 13 | 1.350 | 1.771 | 2.160 | 2.650 | 3.012 | 4.221 |
| 14 | 1.345 | 1.761 | 2.145 | 2.624 | 2.977 | 4.140 |
| 15 | 1.341 | 1.753 | 2.131 | 2.602 | 2.947 | 4.073 |
| 16 | 1.337 | 1.746 | 2.120 | 2.583 | 2.921 | 4.015 |
| 17 | 1.333 | 1.740 | 2.110 | 2.567 | 2.898 | 3.965 |
| 18 | 1.330 | 1.734 | 2.101 | 2.552 | 2.878 | 3.922 |
| 19 | 1.328 | 1.729 | 2.093 | 2.539 | 2.861 | 3.883 |
| 20 | 1.325 | 1.725 | 2.086 | 2.528 | 2.845 | 3.850 |
| 21 | 1.323 | 1.721 | 2.080 | 2.518 | 2.831 | 3.819 |
| 22 | 1.321 | 1.717 | 2.074 | 2.508 | 2.819 | 3.792 |
| 23 | 1.319 | 1.714 | 2.069 | 2.500 | 2.807 | 3.768 |
| 24 | 1.318 | 1.711 | 2.064 | 2.492 | 2.797 | 3.745 |
| 25 | 1.316 | 1.708 | 2.060 | 2.485 | 2.787 | 3.725 |
| 26 | 1.315 | 1.706 | 2.056 | 2.479 | 2.779 | 3.707 |
| 27 | 1.314 | 1.703 | 2.052 | 2.473 | 2.771 | 3.690 |
| 28 | 1.313 | 1.701 | 2.048 | 2.467 | 2.763 | 3.674 |
| 29 | 1.311 | 1.699 | 2.045 | 2.462 | 2.756 | 3.659 |
| 30 | 1.310 | 1.697 | 2.042 | 2.457 | 2.750 | 3.646 |
| 40 | 1.303 | 1.684 | 2.021 | 2.423 | 2.704 | 3.551 |
| 60 | 1.296 | 1.671 | 2.000 | 2.390 | 2.660 | 3.460 |
| 120 | 1.289 | 1.658 | 1.980 | 2.358 | 2.617 | 3.373 |
| ∞ | 1.282 | 1.645 | 1.960 | 2.326 | 2.576 | 3.291 |

APPENDIX G

*Critical Values of the F Distribution
at a 1 Percent Level of Significance*

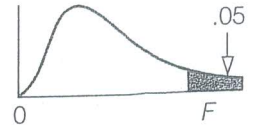


Degrees of Freedom for the Numerator

| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 12 | 15 | 20 | 24 | 30 | 40 |
|-----|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| 1 | 4052 | 5000 | 5403 | 5625 | 5764 | 5859 | 5928 | 5981 | 6022 | 6056 | 6106 | 6157 | 6209 | 6235 | 6261 | 6287 |
| 2 | 98.5 | 99.0 | 99.2 | 99.2 | 99.3 | 99.3 | 99.4 | 99.4 | 99.4 | 99.4 | 99.4 | 99.4 | 99.4 | 99.5 | 99.5 | 99.5 |
| 3 | 34.1 | 30.8 | 29.5 | 28.7 | 28.2 | 27.9 | 27.7 | 27.5 | 27.3 | 27.2 | 27.1 | 26.9 | 26.7 | 26.6 | 26.5 | 26.4 |
| 4 | 21.2 | 18.0 | 16.7 | 16.0 | 15.5 | 15.2 | 15.0 | 14.8 | 14.7 | 14.5 | 14.4 | 14.2 | 14.0 | 13.9 | 13.8 | 13.7 |
| 5 | 16.3 | 13.3 | 12.1 | 11.4 | 11.0 | 10.7 | 10.5 | 10.3 | 10.2 | 10.1 | 9.89 | 9.72 | 9.55 | 9.47 | 9.38 | 9.29 |
| 6 | 13.7 | 10.9 | 9.78 | 9.15 | 8.75 | 8.47 | 8.26 | 8.10 | 7.98 | 7.87 | 7.72 | 7.56 | 7.40 | 7.31 | 7.23 | 7.14 |
| 7 | 12.2 | 9.55 | 8.45 | 7.85 | 7.46 | 7.19 | 6.99 | 6.84 | 6.72 | 6.62 | 6.47 | 6.31 | 6.16 | 6.07 | 5.99 | 5.91 |
| 8 | 11.3 | 8.65 | 7.59 | 7.01 | 6.63 | 6.37 | 6.18 | 6.03 | 5.91 | 5.81 | 5.67 | 5.52 | 5.36 | 5.28 | 5.20 | 5.12 |
| 9 | 10.6 | 8.02 | 6.99 | 6.42 | 6.06 | 5.80 | 5.61 | 5.47 | 5.35 | 5.26 | 5.11 | 4.96 | 4.81 | 4.73 | 4.65 | 4.57 |
| 10 | 10.0 | 7.56 | 6.55 | 5.99 | 5.64 | 5.39 | 5.20 | 5.06 | 4.94 | 4.85 | 4.71 | 4.56 | 4.41 | 4.33 | 4.25 | 4.17 |
| 11 | 9.65 | 7.21 | 6.22 | 5.67 | 5.32 | 5.07 | 4.89 | 4.74 | 4.63 | 4.54 | 4.40 | 4.25 | 4.10 | 4.02 | 3.94 | 3.86 |
| 12 | 9.33 | 6.93 | 5.95 | 5.41 | 5.06 | 4.82 | 4.64 | 4.50 | 4.39 | 4.30 | 4.16 | 4.01 | 3.86 | 3.78 | 3.70 | 3.62 |
| 13 | 9.07 | 6.70 | 5.74 | 5.21 | 4.86 | 4.62 | 4.44 | 4.30 | 4.19 | 4.10 | 3.96 | 3.82 | 3.66 | 3.59 | 3.51 | 3.43 |
| 14 | 8.86 | 6.51 | 5.56 | 5.04 | 4.69 | 4.46 | 4.28 | 4.14 | 4.03 | 3.94 | 3.80 | 3.66 | 3.51 | 3.43 | 3.35 | 3.27 |
| 15 | 8.68 | 6.36 | 5.42 | 4.89 | 4.56 | 4.32 | 4.14 | 4.00 | 3.89 | 3.80 | 3.67 | 3.52 | 3.37 | 3.29 | 3.21 | 3.13 |
| 16 | 8.53 | 6.23 | 5.29 | 4.77 | 4.44 | 4.20 | 4.03 | 3.89 | 3.78 | 3.69 | 3.55 | 3.41 | 3.26 | 3.18 | 3.10 | 3.02 |
| 17 | 8.40 | 6.11 | 5.18 | 4.67 | 4.34 | 4.10 | 3.93 | 3.79 | 3.68 | 3.59 | 3.46 | 3.31 | 3.16 | 3.08 | 3.00 | 2.92 |
| 18 | 8.29 | 6.01 | 5.09 | 4.58 | 4.25 | 4.01 | 3.84 | 3.71 | 3.60 | 3.51 | 3.37 | 3.23 | 3.08 | 3.00 | 2.92 | 2.84 |
| 19 | 8.18 | 5.93 | 5.01 | 4.50 | 4.17 | 3.94 | 3.77 | 3.63 | 3.52 | 3.43 | 3.30 | 3.15 | 3.00 | 2.92 | 2.84 | 2.76 |
| 20 | 8.10 | 5.85 | 4.94 | 4.43 | 4.10 | 3.87 | 3.70 | 3.56 | 3.46 | 3.37 | 3.23 | 3.09 | 2.94 | 2.86 | 2.78 | 2.69 |
| 21 | 8.02 | 5.78 | 4.87 | 4.37 | 4.04 | 3.81 | 3.64 | 3.51 | 3.40 | 3.31 | 3.17 | 3.03 | 2.88 | 2.80 | 2.72 | 2.64 |
| 22 | 7.95 | 5.72 | 4.82 | 4.31 | 3.99 | 3.76 | 3.59 | 3.45 | 3.35 | 3.26 | 3.12 | 2.98 | 2.83 | 2.75 | 2.67 | 2.58 |
| 23 | 7.88 | 5.66 | 4.76 | 4.26 | 3.94 | 3.71 | 3.54 | 3.41 | 3.30 | 3.21 | 3.07 | 2.93 | 2.78 | 2.70 | 2.62 | 2.54 |
| 24 | 7.82 | 5.61 | 4.72 | 4.22 | 3.90 | 3.67 | 3.50 | 3.36 | 3.26 | 3.17 | 3.03 | 2.89 | 2.74 | 2.66 | 2.58 | 2.49 |
| 25 | 7.77 | 5.57 | 4.68 | 4.18 | 3.85 | 3.63 | 3.46 | 3.32 | 3.22 | 3.13 | 2.99 | 2.85 | 2.70 | 2.62 | 2.54 | 2.45 |
| 30 | 7.56 | 5.39 | 4.51 | 4.02 | 3.70 | 3.47 | 3.30 | 3.17 | 3.07 | 2.98 | 2.84 | 2.70 | 2.55 | 2.47 | 2.39 | 2.30 |
| 40 | 7.31 | 5.18 | 4.31 | 3.83 | 3.51 | 3.29 | 3.12 | 2.99 | 2.89 | 2.80 | 2.66 | 2.52 | 2.37 | 2.29 | 2.20 | 2.11 |
| 60 | 7.08 | 4.98 | 4.13 | 3.65 | 3.34 | 3.12 | 2.95 | 2.82 | 2.72 | 2.63 | 2.50 | 2.35 | 2.20 | 2.12 | 2.03 | 1.94 |
| 120 | 6.85 | 4.79 | 3.95 | 3.48 | 3.17 | 2.96 | 2.79 | 2.66 | 2.56 | 2.47 | 2.34 | 2.19 | 2.03 | 1.95 | 1.86 | 1.76 |
| ∞ | 6.63 | 4.61 | 3.78 | 3.32 | 3.02 | 2.80 | 2.64 | 2.51 | 2.41 | 2.32 | 2.18 | 2.04 | 1.88 | 1.79 | 1.70 | 1.59 |

APPENDIX G

Critical Values of the F Distribution at a 5 Percent Level of Significance



| | | Degrees of Freedom for the Numerator | | | | | | | | | | | | | | | |
|--|------|--------------------------------------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 12 | 15 | 20 | 24 | 30 | 40 |
| Degrees of Freedom for the Denominator | 1 | 161 | 200 | 216 | 225 | 230 | 234 | 237 | 239 | 241 | 242 | 244 | 246 | 248 | 249 | 250 | 251 |
| | 2 | 18.5 | 19.0 | 19.2 | 19.2 | 19.3 | 19.3 | 19.4 | 19.4 | 19.4 | 19.4 | 19.4 | 19.4 | 19.4 | 19.5 | 19.5 | 19.5 |
| | 3 | 10.1 | 9.55 | 9.28 | 9.12 | 9.01 | 8.94 | 8.89 | 8.85 | 8.81 | 8.79 | 8.74 | 8.70 | 8.66 | 8.64 | 8.62 | 8.59 |
| | 4 | 7.71 | 6.94 | 6.59 | 6.39 | 6.26 | 6.16 | 6.09 | 6.04 | 6.00 | 5.96 | 5.91 | 5.86 | 5.80 | 5.77 | 5.75 | 5.72 |
| | 5 | 6.61 | 5.79 | 5.41 | 5.19 | 5.05 | 4.95 | 4.88 | 4.82 | 4.77 | 4.74 | 4.68 | 4.62 | 4.56 | 4.53 | 4.50 | 4.46 |
| | 6 | 5.99 | 5.14 | 4.76 | 4.53 | 4.39 | 4.28 | 4.21 | 4.15 | 4.10 | 4.06 | 4.00 | 3.94 | 3.87 | 3.84 | 3.81 | 3.77 |
| | 7 | 5.59 | 4.74 | 4.35 | 4.12 | 3.97 | 3.87 | 3.79 | 3.73 | 3.68 | 3.64 | 3.57 | 3.51 | 3.44 | 3.41 | 3.38 | 3.34 |
| | 8 | 5.32 | 4.46 | 4.07 | 3.84 | 3.69 | 3.58 | 3.50 | 3.44 | 3.39 | 3.35 | 3.28 | 3.22 | 3.15 | 3.12 | 3.08 | 3.04 |
| | 9 | 5.12 | 4.26 | 3.86 | 3.63 | 3.48 | 3.37 | 3.29 | 3.23 | 3.18 | 3.14 | 3.07 | 3.01 | 2.94 | 2.90 | 2.86 | 2.83 |
| | 10 | 4.96 | 4.10 | 3.71 | 3.48 | 3.33 | 3.22 | 3.14 | 3.07 | 3.02 | 2.98 | 2.91 | 2.85 | 2.77 | 2.74 | 2.70 | 2.66 |
| | 11 | 4.84 | 3.98 | 3.59 | 3.36 | 3.20 | 3.09 | 3.01 | 2.95 | 2.90 | 2.85 | 2.79 | 2.72 | 2.65 | 2.61 | 2.57 | 2.53 |
| | 12 | 4.75 | 3.89 | 3.49 | 3.26 | 3.11 | 3.00 | 2.91 | 2.85 | 2.80 | 2.75 | 2.69 | 2.62 | 2.54 | 2.51 | 2.47 | 2.43 |
| | 13 | 4.67 | 3.81 | 3.41 | 3.18 | 3.03 | 2.92 | 2.83 | 2.77 | 2.71 | 2.67 | 2.60 | 2.53 | 2.46 | 2.42 | 2.38 | 2.34 |
| | 14 | 4.60 | 3.74 | 3.34 | 3.11 | 2.96 | 2.85 | 2.76 | 2.70 | 2.65 | 2.60 | 2.53 | 2.46 | 2.39 | 2.35 | 2.31 | 2.27 |
| | 15 | 4.54 | 3.68 | 3.29 | 3.06 | 2.90 | 2.79 | 2.71 | 2.64 | 2.59 | 2.54 | 2.48 | 2.40 | 2.33 | 2.29 | 2.25 | 2.20 |
| | 16 | 4.49 | 3.63 | 3.24 | 3.01 | 2.85 | 2.74 | 2.66 | 2.59 | 2.54 | 2.49 | 2.42 | 2.35 | 2.28 | 2.24 | 2.19 | 2.15 |
| | 17 | 4.45 | 3.59 | 3.20 | 2.96 | 2.81 | 2.70 | 2.61 | 2.55 | 2.49 | 2.45 | 2.38 | 2.31 | 2.23 | 2.19 | 2.15 | 2.10 |
| | 18 | 4.41 | 3.55 | 3.16 | 2.93 | 2.77 | 2.66 | 2.58 | 2.51 | 2.46 | 2.41 | 2.34 | 2.27 | 2.19 | 2.15 | 2.11 | 2.06 |
| | 19 | 4.38 | 3.52 | 3.13 | 2.90 | 2.74 | 2.63 | 2.54 | 2.48 | 2.42 | 2.38 | 2.31 | 2.23 | 2.16 | 2.11 | 2.07 | 2.03 |
| | 20 | 4.35 | 3.49 | 3.10 | 2.87 | 2.71 | 2.60 | 2.51 | 2.45 | 2.39 | 2.35 | 2.28 | 2.20 | 2.12 | 2.08 | 2.04 | 1.99 |
| | 21 | 4.32 | 3.47 | 3.07 | 2.84 | 2.68 | 2.57 | 2.49 | 2.42 | 2.37 | 2.32 | 2.25 | 2.18 | 2.10 | 2.05 | 2.01 | 1.96 |
| | 22 | 4.30 | 3.44 | 3.05 | 2.82 | 2.66 | 2.55 | 2.46 | 2.40 | 2.34 | 2.30 | 2.23 | 2.15 | 2.07 | 2.03 | 1.98 | 1.94 |
| | 23 | 4.28 | 3.42 | 3.03 | 2.80 | 2.64 | 2.53 | 2.44 | 2.37 | 2.32 | 2.27 | 2.20 | 2.13 | 2.05 | 2.01 | 1.96 | 1.91 |
| | 24 | 4.26 | 3.40 | 3.01 | 2.78 | 2.62 | 2.51 | 2.42 | 2.36 | 2.30 | 2.25 | 2.18 | 2.11 | 2.03 | 1.98 | 1.94 | 1.89 |
| | 25 | 4.24 | 3.39 | 2.99 | 2.76 | 2.60 | 2.49 | 2.40 | 2.34 | 2.28 | 2.24 | 2.16 | 2.09 | 2.01 | 1.96 | 1.92 | 1.87 |
| 30 | 4.17 | 3.32 | 2.92 | 2.69 | 2.53 | 2.42 | 2.33 | 2.27 | 2.21 | 2.16 | 2.09 | 2.01 | 1.93 | 1.89 | 1.84 | 1.79 | |
| 40 | 4.08 | 3.23 | 2.84 | 2.61 | 2.45 | 2.34 | 2.25 | 2.18 | 2.12 | 2.08 | 2.00 | 1.92 | 1.84 | 1.79 | 1.74 | 1.69 | |
| 60 | 4.00 | 3.15 | 2.76 | 2.53 | 2.37 | 2.25 | 2.17 | 2.10 | 2.04 | 1.99 | 1.92 | 1.84 | 1.75 | 1.70 | 1.65 | 1.59 | |
| 120 | 3.92 | 3.07 | 2.68 | 2.45 | 2.29 | 2.18 | 2.09 | 2.02 | 1.96 | 1.91 | 1.83 | 1.75 | 1.66 | 1.61 | 1.55 | 1.50 | |
| ∞ | 3.84 | 3.00 | 2.60 | 2.37 | 2.21 | 2.10 | 2.01 | 1.94 | 1.88 | 1.83 | 1.75 | 1.67 | 1.57 | 1.52 | 1.46 | 1.39 | |

APPENDIX J

Data Set 1 — Real Estate

| | x_1 | x_2 | x_3 | x_4 | x_5 | x_6 | x_7 | x_8 |
|--|----------|-------|---------|-------|-------|-------|-------|-------|
| x_1 = Selling price in \$000 | | | | | | | | |
| x_2 = Number of bedrooms | | | | | | | | |
| x_3 = Size of the home in square feet | | | | | | | | |
| x_4 = Pool (1 = yes, 0 = no) | | | | | | | | |
| x_5 = Distance from the center of the city | | | | | | | | |
| x_6 = Township | | | | | | | | |
| x_7 = Garage attached (1 = yes, 0 = no) | | | | | | | | |
| x_8 = Number of bathrooms | | | | | | | | |
| | 182.655 | 4 | 2,023 | 0 | 14 | 4 | 0 | 2.5 |
| | 216 | 4 | 2,310 | 1 | 19 | 2 | 0 | 2 |
| | 312.12 | 6 | 2,639 | 1 | 7 | 5 | 1 | 2.5 |
| | 199.8 | 3 | 2,069 | 1 | 19 | 3 | 1 | 2 |
| | 273.24 | 5 | 2,182 | 1 | 16 | 2 | 1 | 3 |
| | 206.01 | 3 | 2,090 | 0 | 9 | 3 | 0 | 1.5 |
| | 232.2 | 3 | 1,928 | 0 | 16 | 1 | 1 | 1.5 |
| | 198.315 | 4 | 2,056 | 0 | 19 | 1 | 1 | 1.5 |
| | 205.065 | 3 | 2,012 | 0 | 20 | 4 | 0 | 2 |
| | 175.635 | 4 | 2,262 | 0 | 24 | 4 | 1 | 2 |
| | 307.8 | 3 | 2,431 | 0 | 21 | 2 | 1 | 3 |
| | 269.19 | 5 | 2,217 | 1 | 8 | 5 | 1 | 3 |
| | 224.775 | 3 | 2,157 | 1 | 17 | 1 | 1 | 2.5 |
| | 171.585 | 3 | 2,014 | 0 | 16 | 4 | 0 | 2 |
| | 216.81 | 3 | 2,221 | 1 | 15 | 1 | 1 | 2 |
| | 192.645 | 6 | 2,236 | 0 | 14 | 1 | 0 | 2 |
| | 236.385 | 5 | 2,189 | 1 | 20 | 3 | 1 | 2 |
| | 172.395 | 3 | 2,218 | 1 | 23 | 3 | 0 | 2 |
| | 251.37 | 3 | 1,937 | 1 | 12 | 2 | 1 | 2 |
| | 245.97 | 6 | 2,296 | 1 | 7 | 3 | 1 | 3 |
| | 147.42 | 6 | 1,749 | 0 | 12 | 1 | 0 | 2 |
| | 176.04 | 4 | 2,230 | 1 | 15 | 1 | 1 | 2 |
| | 228.42 | 3 | 2,263 | 1 | 17 | 5 | 1 | 1.5 |
| | 166.455 | 3 | 1,593 | 0 | 19 | 3 | 0 | 2.5 |
| | 189.405 | 4 | 2,221 | 1 | 24 | 1 | 1 | 2 |
| | 312.12 | 7 | 2,403 | 1 | 13 | 3 | 1 | 3 |
| | 289.845 | 6 | 2,036 | 1 | 21 | 3 | 1 | 3 |
| | 269.865 | 5 | 2,170 | 0 | 11 | 4 | 1 | 2.5 |
| | 154.305 | 2 | 2,007 | 1 | 13 | 2 | 0 | 2 |
| | 222.075 | 2 | 2,054 | 1 | 9 | 5 | 1 | 2 |
| | 209.655 | 5 | 2,247 | 0 | 13 | 2 | 1 | 2 |
| | 190.89 | 3 | 2,190 | 0 | 18 | 3 | 1 | 2 |
| | 254.34 | 4 | 2,495 | 0 | 15 | 3 | 1 | 2 |
| | 207.495 | 3 | 2,080 | 0 | 10 | 2 | 0 | 2 |
| | 209.655 | 4 | 2,210 | 0 | 19 | 2 | 1 | 2 |
| | 294.03 | 2 | 2,133 | 1 | 13 | 2 | 1 | 2.5 |
| | 176.31 | 2 | 2,037 | 0 | 17 | 3 | 0 | 2 |
| | 294.3 | 7 | 2,448 | 1 | 8 | 4 | 1 | 2 |
| | 223.965 | 3 | 1,900 | 0 | 6 | 1 | 1 | 2 |
| | 125.01 | 2 | 1,871 | 1 | 18 | 4 | 0 | 1.5 |
| | 236.8035 | 4 | 2,593.9 | 0 | 17 | 5 | 1 | 2 |
| | 164.1465 | 4 | 2,312.2 | 1 | 19 | 4 | 0 | 2 |
| | 217.8495 | 3 | 2,498.1 | 1 | 12 | 3 | 0 | 2 |
| | 192.213 | 2 | 2,406.8 | 1 | 16 | 2 | 0 | 2.5 |
| | 125.874 | 2 | 2,362.8 | 1 | 28 | 1 | 0 | 1.5 |
| | 220.887 | 2 | 2,328.7 | 0 | 12 | 1 | 1 | 2 |